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Tests of general relativity

Tests of general relativity serve to establish observational evidence for the theory of general relativity. The first three tests, proposed by Einstein in 1915, concerned the "anomalous" precession of the perihelion of Mercury, the bending of light in gravitational fields, and the gravitational redshift. The precession of Mercury was already known; experiments showing light bending in line with the predictions of general relativity was found in 1919, with increasing precision measurements done in subsequent tests, and astrophysical measurement of the gravitational redshift was claimed to be measured in 1925, although measurements sensitive enough to actually confirm the theory were not done until 1954. A program of more accurate tests starting in 1959 tested the various predictions of general relativity with a further degree of accuracy in the weak gravitational field limit, severely limiting possible deviations from the theory.

In the 1970s, additional tests began to be made, starting with Irwin Shapiro's measurement of the relativistic time delay in radar signal travel time near the sun. Beginning in 1974, <u>Hulse</u>, <u>Taylor</u> and others have studied the behaviour of <u>binary pulsars</u> experiencing much stronger gravitational fields than those found in the Solar System. Both in the weak field limit (as in the Solar System) and with the stronger fields present in systems of binary pulsars the predictions of general relativity have been extremely well tested locally.

In February 2016, the <u>Advanced LIGO</u> team announced that they had <u>directly detected gravitational waves</u> from a black hole merger. ^[1] This discovery, along with additional detections announced in June 2016 and June 2017, ^[2] tested general relativity in the very strong field limit, observing to date no deviations from theory.

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Classical tests

Albert Einstein proposed^{[3][4]} three tests of general relativity, subsequently called **the classical tests of general relativity**, in 1916:

- 1. the perihelion precession of Mercury's orbit
- 2. the deflection of light by the Sun
- 3. the gravitational redshift of light

In the letter to the <u>London Times</u> on November 28, 1919, he described the theory of relativity and thanked his English colleagues for their understanding and testing of his work. He also mentioned three classical tests with comments:^[5]

"The chief attraction of the theory lies in its logical completeness. If a single one of the conclusions drawn from it proves wrong, it must be given up; to modify it without destroying the whole structure seems to be impossible."

Perihelion precession of Mercury

Under Newtonian physics, a two-body system consisting of a lone object orbiting a spherical mass would trace out an <u>ellipse</u> with the spherical mass at a <u>focus</u>. The point of closest approach, called the <u>periapsis</u> (or, because the central body in the Solar System is the Sun, <u>perihelion</u>), is fixed. A number of effects in the Solar System cause the perihelia of planets to precess (rotate) around the Sun. The principal cause is the presence of other planets which <u>perturb</u> one another's orbit. Another (much less significant) effect is solar oblateness.

Mercury deviates from the precession predicted from these Newtonian effects. This anomalous rate of precession of the perihelion of Mercury's orbit was first recognized in 1859 as a problem in <u>celestial mechanics</u>, by <u>Urbain Le Verrier</u>. His reanalysis of available timed observations of transits of <u>Mercury</u> over the Sun's disk from 1697 to 1848 showed that the actual rate of the precession disagreed from that predicted from Newton's theory by 38" (<u>arc seconds</u>) per <u>tropical century</u> (later re-estimated at 43" by <u>Simon Newcomb</u> in 1882). ^[6] A number of *ad hoc* and ultimately unsuccessful solutions were proposed, but they tended to introduce more problems.

In general relativity, this remaining <u>precession</u>, or change of orientation of the orbital ellipse within its orbital plane, is explained by gravitation being mediated by the curvature of spacetime. Einstein showed that general relativity^[3] agrees closely with the observed amount of perihelion shift. This was a powerful factor motivating the adoption of general relativity. Recently, Friedman and Steiner^[7] obtained the observed perihelion shift and explained its origin without curving spacetime using the <u>relativistic Newtonian dynamics</u> model.

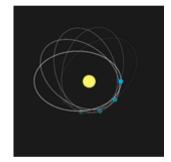
Although earlier measurements of planetary orbits were made using conventional telescopes, more accurate measurements are now made with <u>radar</u>. The total observed precession of Mercury is $574.10''\pm0.65$ per century^[8] relative to the inertial <u>ICRF</u>. This precession can be attributed to the following causes:

Sources of the precession of perihelion for Mercury

Amount (arcsec/Julian century) ^[9]	Cause
532.3035	Gravitational tugs of other solar bodies
0.0286	Oblateness of the Sun (quadrupole moment)
42.9799	Gravitoelectric effects (Schwarzschild-like)
-0.0020	Lense–Thirring precession
575.31	Total predicted
574.10±0.65 ^[8]	Observed



Transit of Mercury on November 8, 2006 with sunspots #921, 922, and 923



The perihelion precession of Mercury

The correction by 42.98" is 3/2 multiple of classical prediction with <u>PPN parameters</u> $\gamma = \beta = 1$. Thus the effect can be fully explained by general relativity. More recent calculations based on more precise measurements have not materially changed the situation.

In general relativity the perihelion shift σ , expressed in radians per revolution, is approximately given by:^[11]

$$\sigma = rac{24 \pi^3 L^2}{T^2 c^2 (1-e^2)} \; ,$$

where L is the <u>semi-major axis</u>, T is the <u>orbital period</u>, c is the speed of light, and e is the <u>orbital eccentricity</u> (see: <u>Two-body problem in general relativity</u>). This formula gives the exact expression for the perihelion shift derived in relativistic Newtonian dynamics. [12]

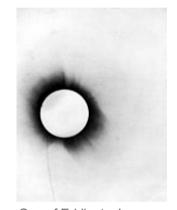
The other planets experience perihelion shifts as well, but, since they are farther from the Sun and have longer periods, their shifts are lower, and could not be observed accurately until long after Mercury's. For example, the perihelion shift of Earth's orbit due to general relativity is of 3.84" per century, and Venus's is 8.62". Both values have now been measured, with results in good agreement with theory. The periapsis shift has also now been measured for binary pulsar systems, with PSR 1913+16 amounting to 4.2° per year. These observations are consistent with general relativity. It is also possible to measure periapsis shift in binary star systems which do not contain ultra-dense stars, but it is more difficult to model the classical effects precisely – for example, the alignment of the stars' spin to their orbital plane needs to be known and is hard to measure directly. A few systems, such as DI Herculis, In have been measured as test cases for general relativity.

Deflection of light by the Sun

Henry Cavendish in 1784 (in an unpublished manuscript) and Johann Georg von Soldner in 1801 (published in 1804) had pointed out that Newtonian gravity predicts that starlight will bend around a massive object. [17][18] The same value as Soldner's was calculated by Einstein in 1911 based on the equivalence principle alone. However, Einstein noted in 1915 in the process of completing general relativity, that his (and thus Soldner's) 1911 result is only half of the correct value. Einstein became the first to calculate the correct value for light bending. [19]

The first observation of light deflection was performed by noting the change in position of <u>stars</u> as they passed near the Sun on the <u>celestial sphere</u>. The observations were performed by <u>Arthur Eddington</u> and his collaborators during the total <u>solar eclipse of May 29, 1919</u>, [20] when the stars near the Sun (at that time in the constellation <u>Taurus</u>) could be observed. [20] Observations were made simultaneously in the cities of <u>Sobral, Ceará</u>, Brazil and in <u>São Tomé and Príncipe</u> on the west coast of Africa. [21] The result was considered spectacular news and made the front page of most major newspapers. It made Einstein and his theory of general relativity world-famous. When asked by his assistant what his reaction would have been if general relativity had not been confirmed by Eddington and Dyson in 1919, Einstein famously made the quip: "Then I would feel sorry for the dear Lord. The theory is correct anyway." [22]

The early accuracy, however, was poor. The results were argued by $some^{[23]}$ to have been plagued by systematic error and possibly confirmation bias, although modern reanalysis of the dataset suggests that Eddington's analysis was accurate. The measurement was repeated by a team from the Lick Observatory in the 1922 eclipse, with results that agreed with the 1919 results and has been



One of Eddington's photographs of the 1919 solar eclipse experiment presented in his 1920 paper announcing its success

repeated several times since, most notably in 1953 by Yerkes Observatory astronomers^[27] and in 1973 by a team from the University of Texas.^[28] Considerable uncertainty remained in these measurements for almost fifty years, until observations started being made at radio frequencies.^[29] While the Sun is too close by for an Einstein ring to lie outside its corona, such a ring formed by the deflection of light from distant galaxies has been observed for a nearby star.^[30]

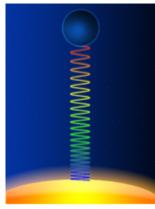
Gravitational redshift of light

Einstein predicted the gravitational redshift of light from the equivalence principle in 1907, and it was predicted that this effect might be measured in the spectral lines of a white dwarf star, which has a very high gravitational field. Initial attempts to measure the gravitational redshift of the spectrum of Sirius-B, were done by Walter Sydney Adams in 1925, but the result was criticized as being unusable due to the contamination from light from the (much brighter) primary star, Sirius. [31][32] The first accurate measurement of the gravitational redshift of a white dwarf was done by Popper in 1954, measuring a 21 km/sec gravitational redshift of 40 Eridani B. [32]

The redshift of Sirius B was finally measured by Greenstein *et al.* in 1971, obtaining the value for the gravitational redshift of 89±19 km/sec, with more accurate measurements by the Hubble Space Telescope showing 80.4±4.8 km/sec.

Tests of Special Relativity

The general theory of relativity incorporates Einstein's <u>special theory of relativity</u>, and hence test of special relativity are also testing aspects of general relativity. As a consequence of the <u>equivalence principle</u>, <u>Lorentz invariance</u> holds locally in non-rotating, freely falling reference frames. Experiments related to Lorentz invariance special relativity (that is, when gravitational effects can be neglected) are described in Tests of special relativity.



The gravitational redshift of a light wave as it moves upwards against a gravitational field (caused by the yellow star below).

Modern tests

The modern era of testing general relativity was ushered in largely at the impetus of <u>Dicke</u> and <u>Schiff</u> who laid out a framework for testing general relativity. [33][34][35] They emphasized the importance not only of the classical tests, but of null experiments, testing for effects which in principle could occur in a theory of gravitation, but do not occur in general relativity. Other important theoretical developments included the inception of <u>alternative theories</u> to general relativity, in particular, <u>scalar-tensor theories</u> such as the <u>Brans-Dicke theory</u>; [36] the <u>parameterized post-Newtonian formalism</u> in which deviations from general relativity can be quantified; and the framework of the equivalence principle.

Experimentally, new developments in <u>space exploration</u>, <u>electronics</u> and <u>condensed matter physics</u> have made additional precise experiments possible, such as the Pound–Rebka experiment, laser interferometry and lunar rangefinding.

Post-Newtonian tests of gravity

Early tests of general relativity were hampered by the lack of viable competitors to the theory: it was not clear what sorts of tests would distinguish it from its competitors. General relativity was the only known relativistic theory of gravity compatible with special relativity and observations. Moreover, it is an extremely simple and elegant theory. This changed with the introduction of <u>Brans-Dicke theory</u> in 1960. This theory is arguably simpler, as it contains no <u>dimensionful</u> constants, and is compatible with a version of <u>Mach's principle</u> and <u>Dirac's large numbers hypothesis</u>, two philosophical ideas which have been influential in the history of relativity. Ultimately, this led to the development of the <u>parametrized post-Newtonian formalism</u> by <u>Nordtvedt</u> and <u>Will</u>, which parametrizes, in terms of ten adjustable parameters, all the possible departures from Newton's law of universal gravitation to first order in the velocity of moving objects (*i.e.* to first order in v/c,

where v is the velocity of an object and c is the speed of light). This approximation allows the possible deviations from general relativity, for slowly moving objects in weak gravitational fields, to be systematically analyzed. Much effort has been put into constraining the post-Newtonian parameters, and deviations from general relativity are at present severely limited.

The experiments testing gravitational lensing and light time delay limits the same post-Newtonian parameter, the so-called Eddington parameter γ , which is a straightforward parametrization of the amount of deflection of light by a gravitational source. It is equal to one for general relativity, and takes different values in other theories (such as Brans-Dicke theory). It is the best constrained of the ten post-Newtonian parameters, but there are other experiments designed to constrain the others. Precise observations of the perihelion shift of Mercury constrain other parameters, as do tests of the strong equivalence principle.

One of the goals of the mission <u>BepiColombo</u> is testing the general relativity theory by measuring the parameters gamma and beta of the parametrized post-Newtonian formalism with high accuracy.^[37]

Gravitational lensing

One of the most important tests is gravitational lensing. It has been observed in distant astrophysical sources, but these are poorly controlled and it is uncertain how they constrain general relativity. The most precise tests are analogous to Eddington's 1919 experiment: they measure the deflection of radiation from a distant source by the Sun. The sources that can be most precisely analyzed are distant radio sources. In particular, some quasars are very strong radio sources. The directional resolution of any telescope is in principle limited by diffraction; for radio telescopes this is also the practical limit. An important improvement in obtaining positional high accuracies (from milli-arcsecond to micro-arcsecond) was obtained by combining radio telescopes across Earth. The technique is called very long baseline interferometry (VLBI). With this technique radio observations couple the phase information of the radio signal observed in telescopes separated over large distances. Recently, these telescopes have measured the deflection of radio waves by the Sun to extremely high precision, confirming the amount of deflection predicted by general relativity aspect to the 0.03% level. At this level of precision systematic effects have to be carefully taken into account to determine the precise location of the telescopes on Earth. Some important effects are Earth's nutation, rotation, atmospheric refraction, tectonic displacement and tidal waves. Another important effect is refraction of the radio waves by the solar corona. Fortunately, this effect has a characteristic spectrum, whereas gravitational distortion is independent of wavelength. Thus, careful analysis, using measurements at several frequencies, can subtract this source of error.

The entire sky is slightly distorted due to the gravitational deflection of light caused by the Sun (the anti-Sun direction excepted). This effect has been observed by the European Space Agency astrometric satellite Hipparcos. It measured the positions of about 10^5 stars. During the full mission about 3.5×10^6 relative positions have been determined, each to an accuracy of typically 3 milliarcseconds (the accuracy for an 8–9 magnitude star). Since the gravitation deflection perpendicular to the Earth–Sun direction is already 4.07 milliarcseconds, corrections are needed for practically all stars. Without systematic effects, the error in an individual observation of 3 milliarcseconds, could be reduced by the square root of the number of positions, leading to a precision of 0.0016 milliarcseconds. Systematic effects, however, limit the accuracy of the determination to 0.3% (Froeschlé, 1997).

Launched in 2013, the <u>Gaia</u> spacecraft will conduct a census of one billion <u>stars</u> in the <u>Milky Way</u> and measure their positions to an accuracy of 24 microarcseconds. Thus it will also provide stringent new tests of gravitational deflection of light caused by the Sun which was predicted by General relativity. [39]

Light travel time delay testing

Irwin I. Shapiro proposed another test, beyond the classical tests, which could be performed within the Solar System. It is sometimes called the fourth "classical" test of general relativity. He predicted a relativistic time delay (Shapiro delay) in the round-trip travel time for radar signals reflecting off other planets. [40] The mere curvature of the path of a photon passing near the Sun is too small to have an observable delaying effect (when the round-trip time is compared to the time taken if the photon had followed a straight path), but general relativity predicts a time delay that becomes progressively larger when the photon passes nearer to the Sun due to the time dilation in the gravitational potential of the Sun. Observing radar reflections from Mercury and Venus just before and after it is eclipsed by the Sun agrees with general relativity theory at the 5% level. [41] More recently, the Cassini probe has undertaken a similar experiment which gave agreement with general relativity at the 0.002% level [42]. However, the following detailed studies [43][44] revealed that the measured value of the PPN parameter gamma is affected by gravitomagnetic effect caused by the orbital motion of Sun around the barycenter of the solar system. The gravitomagnetic effect in the Cassini radioscience experiment was implicitly postulated by B. Berottti as having a pure general relativistic origin but its theoretical value has been never tested in the experiment which effectively makes the experimental uncertainty in the measured value of gamma actually larger (by a factor of 10) than 0.002% claimed by B. Berotti and co-authors in Nature.

Very Long Baseline Interferometry has measured velocity-dependent (gravitomagnetic) corrections to the Shapiro time delay in the field of moving Jupiter^{[45][46]} and Saturn.^[47]

The equivalence principle

The equivalence principle, in its simplest form, asserts that the trajectories of falling bodies in a gravitational field should be independent of their mass and internal structure, provided they are small enough not to disturb the environment or be affected by <u>tidal forces</u>. This idea has been tested to extremely high precision by <u>Eötvös torsion balance experiments</u>, which look for a differential acceleration between two test masses. Constraints on this, and on the existence of a composition-dependent fifth force or gravitational Yukawa interaction are very strong, and are discussed under fifth force and weak equivalence principle.

A version of the equivalence principle, called the <u>strong equivalence principle</u>, asserts that self-gravitation falling bodies, such as stars, planets or black holes (which are all held together by their gravitational attraction) should follow the same trajectories in a gravitational field, provided the same conditions are satisfied. This is called the <u>Nordtvedt effect</u> and is most precisely tested by the <u>Lunar Laser Ranging Experiment</u>. [48][49] Since 1969, it has continuously measured the distance from several rangefinding stations on Earth to reflectors on the Moon to approximately centimeter accuracy. [50] These have provided a strong constraint on several of the other post-Newtonian parameters.

Another part of the strong equivalence principle is the requirement that Newton's gravitational constant be constant in time, and have the same value everywhere in the universe. There are many independent observations limiting the possible variation of Newton's gravitational constant, ^[51] but one of the best comes from lunar rangefinding which suggests that the gravitational constant does not change by more than one part in 10¹¹ per year. The constancy of the other constants is discussed in the Einstein equivalence principle section of the equivalence principle article.

Gravitational redshift

The first of the classical tests discussed above, the gravitational redshift, is a simple consequence of the Einstein equivalence principle and was predicted by Einstein in 1907. As such, it is not a test of general relativity in the same way as the post-Newtonian tests, because any theory of gravity obeying the equivalence principle should also incorporate the gravitational redshift. Nonetheless, confirming the existence of the effect was an important substantiation of relativistic gravity, since the absence of gravitational redshift would have strongly contradicted relativity. The first observation of the gravitational redshift was the measurement of the shift in the spectral lines from the white dwarf star Sirius B by Adams in 1925, discussed above, and follow-on measurements of other white dwarfs. Because of the difficulty of the astrophysical measurement, however, experimental verification using a known terrestrial source was preferable.

Experimental verification of gravitational redshift using terrestrial sources took several decades, because it is difficult to find clocks (to measure <u>time dilation</u>) or sources of electromagnetic radiation (to measure redshift) with a frequency that is known well enough that the effect can be accurately measured. It was confirmed experimentally for the first time in 1959 using measurements of the change in wavelength of gamma-ray photons generated with the <u>Mössbauer effect</u>, which generates radiation with a very narrow line width. The <u>Pound–Rebka experiment</u> measured the relative redshift of two sources situated at the top and bottom of Harvard University's Jefferson tower. [52][53] The result was in excellent agreement with general relativity. This was one of the first precision experiments testing general relativity. The experiment was later improved to better than the 1% level by Pound and Snider. [54]

The blueshift of a falling photon can be found by assuming it has an equivalent mass based on its frequency E = hf (where h is Planck's constant) along with $E = mc^2$, a result of special relativity. Such simple derivations ignore the fact that in general relativity the experiment compares clock rates, rather than energies. In other words, the "higher energy" of the photon after it falls can be equivalently ascribed to the slower running of clocks deeper in the gravitational potential well. To fully validate general relativity, it is important to also show that the rate of arrival of the photons is greater than the rate at which they are emitted. A very accurate gravitational redshift experiment, which deals with this issue, was performed in 1976, [55] where a hydrogen maser clock on a rocket was launched to a height of 10,000 km, and its rate compared with an identical clock on the ground. It tested the gravitational redshift to 0.007%.

Although the Global Positioning System (GPS) is not designed as a test of fundamental physics, it must account for the gravitational redshift in its timing system, and physicists have analyzed timing data from the GPS to confirm other tests. When the first satellite was launched, some engineers resisted the prediction that a noticeable gravitational time dilation would occur, so the first satellite was launched without the clock adjustment that was later built into subsequent satellites. It showed the predicted shift of 38 microseconds per day. This rate of discrepancy is sufficient to substantially impair function of GPS within hours if not accounted for. An excellent account of the role played by general relativity in the design of GPS can be found in Ashby 2003.^[56]

Other precision tests of general relativity, [57] not discussed here, are the <u>Gravity Probe A</u> satellite, launched in 1976, which showed gravity and velocity affect the ability to synchronize the rates of clocks orbiting a central mass; the <u>Hafele–Keating experiment</u>, which used atomic clocks in circumnavigating aircraft to test general relativity and special relativity together; [58][59] and the forthcoming Satellite Test of the Equivalence Principle.

Frame-dragging tests

Tests of the Lense-Thirring precession, consisting of small secular precessions of the orbit of a test particle in motion around a central rotating mass, for example, a planet or a star, have been performed with the LAGEOS satellites, [60] but many aspects of them remain controversial. The same effect may have been detected in the data of the Mars Global Surveyor (MGS) spacecraft, a former probe in orbit around Mars; also such a test raised a debate. [61] First attempts to detect the Sun's Lense-Thirring effect on the perihelia of the inner planets have been recently reported as well. Frame dragging would cause the orbital plane of stars orbiting near a supermassive black hole to precess about the black hole spin axis. This effect should be detectable within the next few years via astrometric monitoring of stars at the center of the Milky Way galaxy. [62] By comparing the rate of orbital precession of two stars on different orbits, it is possible in principle to test the no-hair theorems of general relativity. [63]



The LAGEOS-1 satellite. (D=60 cm)

The <u>Gravity Probe B</u> satellite, launched in 2004 and operated until 2005, detected frame-dragging and the <u>geodetic effect</u>. The experiment used four quartz spheres the size of ping pong balls coated with a superconductor. Data analysis continued through 2011 due to high noise levels and difficulties in modelling the noise accurately so that a useful signal could be found. Principal investigators at

Stanford University reported on May 4, 2011, that they had accurately measured the frame dragging effect relative to the distant star IM Pegasi, and the calculations proved to be in line with the prediction of Einstein's theory. The results, published in *Physical Review Letters* measured the geodetic effect with an error of about 0.2 percent. The results reported the frame dragging effect (caused by Earth's rotation) added up to 37 milliarcseconds with an error of about 19 percent. [64] Investigator Francis Everitt explained that a milliarcsecond "is the width of a human hair seen at the distance of 10 miles". [65]

In January 2012, <u>LARES</u> satellite was launched on a <u>Vega</u> rocket^[66] to measure <u>Lense-Thirring effect</u> with an accuracy of about 1%, according to its proponents.^[67] This evaluation of the actual accuracy obtainable is a subject of debate.^{[68][69][70]}

Tests of the gravitational potential at small distances

It is possible to test whether the gravitational potential continues with the inverse square law at very small distances. Tests so far have focused on a divergence from GR in the form of a Yukawa potential $V(r) = V_0(1 + \alpha e^{-r/\lambda})$, but no evidence for a potential of this kind has been found. The Yukawa potential with $\alpha = 1$ has been ruled out down to $\lambda = 5.6 \times 10^{-5} \text{m.}^{[71]}$

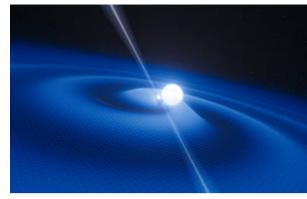
Strong field tests

The very strong gravitational fields that are present close to <u>black holes</u>, especially those <u>supermassive black holes</u> which are thought to power <u>active galactic nuclei</u> and the more active <u>quasars</u>, belong to a field of intense active research. Observations of these quasars and active galactic nuclei are difficult, and interpretation of the observations is heavily dependent upon astrophysical models other than general relativity or competing fundamental <u>theories of gravitation</u>, but they are qualitatively consistent with the black hole concept as modelled in general relativity.

Binary pulsars

<u>Pulsars</u> are rapidly rotating <u>neutron stars</u> which emit regular radio pulses as they rotate. As such they act as clocks which allow very precise monitoring of their orbital motions. Observations of pulsars in orbit around other stars have all demonstrated substantial <u>periapsis</u> precessions that cannot be accounted for classically but can be accounted for by using general relativity. For example, the Hulse–Taylor <u>binary pulsar PSR B1913+16</u> (a pair of neutron stars in which one is detected as a pulsar) has an observed precession of over 4° of arc per year (periastron shift per orbit only about 10⁻⁶). This precession has been used to compute the masses of the components.

Similarly to the way in which atoms and molecules emit electromagnetic radiation, a gravitating mass that is in quadrupole type or higher order vibration, or is asymmetric and in rotation, can emit gravitational waves.^[73] These gravitational waves are predicted to travel at the speed of light. For example, planets orbiting the Sun constantly lose energy via gravitational radiation, but this effect is so small that it is unlikely it will be observed in the near future (Earth radiates about 200 watts (see gravitational waves) of gravitational radiation).



Artist's impression of the pulsar PSR J0348+0432 and its white dwarf companion radiating gravitational waves. [72]

The radiation of gravitational waves has been inferred from the <u>Hulse–Taylor binary</u> (and other binary pulsars).^[74] Precise timing of the pulses shows that the stars orbit only approximately according to <u>Kepler's Laws</u>: over time they gradually spiral towards each other, demonstrating an <u>energy</u> loss in close agreement with the predicted energy radiated by gravitational waves.^{[75][76]} For their discovery of the first binary pulsar and measuring its orbital decay due to gravitational-wave emission, Hulse and Taylor won the 1993 Nobel Prize in Physics.^[77]

A "double pulsar" discovered in 2003, PSR J0737-3039, has a periastron precession of 16.90° per year; unlike the Hulse–Taylor binary, both neutron stars are detected as pulsars, allowing precision timing of both members of the system. Due to this, the tight orbit, the fact that the system is almost edge-on, and the very low transverse velocity of the system as seen from Earth, J0737-3039 provides by far the best system for strong-field tests of general relativity known so far. Several distinct relativistic effects are observed, including orbital decay as in the Hulse–Taylor system. After observing the system for two and a half years, four independent tests of general relativity were possible, the most precise (the Shapiro delay) confirming the general relativity prediction within 0.05%^[78] (nevertheless the periastron shift per orbit is only about 0.0013% of a circle and thus it is not a higher-order relativity test).

In 2013, an international team of astronomers reported new data from observing a pulsar-white dwarf system PSR J0348+0432, in which they have been able to measure a change in the orbital period of 8 millionths of a second per year, and confirmed GR predictions in a regime of extreme gravitational fields never probed before;^[79] but there are still some competing theories that would agree with these data.^[80]

Direct detection of gravitational waves

A number of <u>gravitational-wave detectors</u> have been built with the intent of directly detecting the gravitational waves emanating from such astronomical events as the merger of two <u>neutron stars</u> or <u>black holes</u>. In February 2016, the <u>Advanced LIGO</u> team announced that they had <u>directly detected gravitational waves</u> from a stellar binary black hole merger, [1][81][82] with additional detections announced in June 2016, June 2017, and August 2017. [2][83]

General relativity predicts gravitational waves, as does any theory of gravitation in which changes in the gravitational field propagate at a finite speed.^[84] Since gravitational waves can be directly detected,^{[1][82]} it is possible to use them to learn about the Universe. This is gravitational-wave astronomy. Gravitational-wave astronomy can test general relativity by verifying that the observed waves are of the form predicted (for example, that they only have two transverse polarizations), and by checking that black holes are the objects described by solutions of the Einstein field equations.^{[85][86][87]}

"These amazing observations are the confirmation of a lot of theoretical work, including Einstein's general theory of relativity, which predicts gravitational waves," says physicist Stephen Hawking.^[1]

Cosmological tests

Tests of general relativity on the largest scales are not nearly so stringent as Solar System tests. [88] The earliest such test was prediction and discovery of the expansion of the universe. [89] In 1922, Alexander Friedmann found that Einstein equations have non-stationary solutions (even in the presence of the cosmological constant). [90][91] In 1927, Georges Lemaître showed that static solutions of the Einstein equations, which are possible in the presence of the cosmological constant, are unstable, and therefore the static universe envisioned by Einstein could not exist (it must either expand or contract). [90] Lemaître made an explicit prediction that the universe should expand. [92] He also derived a redshift-distance relationship, which is now known as the Hubble Law. [92] Later, in 1931, Einstein himself agreed with the results of Friedmann and Lemaître. [90] The expansion of the universe discovered by Edwin Hubble in 1929[90] was then considered by many (and continues to be considered by some now) as a direct confirmation of general relativity. [93] In the 1930s, largely due to the work of E. A. Milne, it was realised that the linear relationship between redshift and distance derives from the general assumption of uniformity and isotropy rather than specifically from general relativity. [89] However the prediction of a non-static universe was non-trivial, indeed dramatic, and primarily motivated by general relativity.

Some other cosmological tests include searches for primordial gravitational waves generated during cosmic inflation, which may be detected in the cosmic microwave background polarization [95] or by a proposed space-based gravitational-wave interferometer called the Big Bang Observer. Other tests at high redshift are constraints on other theories of gravity, [96][97] and the variation of the gravitational constant since big bang nucleosynthesis (it varied by no more than 40% since then).

In August 2017, the findings of tests conducted by astronomers using the <u>European Southern Observatory</u>'s <u>Very Large Telescope</u> (VLT), among other instruments, were released, and which positively demonstrated gravitational effects predicted by Albert Einstein. One of which tests observed the orbit of the stars circling around <u>Sagittarius A*</u>, a black hole about 4 million times as massive as the sun. Einstein's theory suggested that large objects bend the space around them, causing other objects to diverge from the straight lines they would otherwise follow. Although previous studies have validated Einstein's theory, this was the first time his theory had been tested on such a gigantic object. The findings were published in *The Astrophysical Journal*. [98][99]

See also

- General relativity
- Tests of special relativity

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Notes

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- the USENET Relativity FAQ experiments page (https://web.archive.org/web/20010711203839/http://www2.corepower.com:8080/~relfaq/experiments.html)
- Mathpages article on Mercury's perihelion shift (http://www.mathpages.com/rr/s6-02/6-02.htm) (for amount of observed and GR shifts).

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